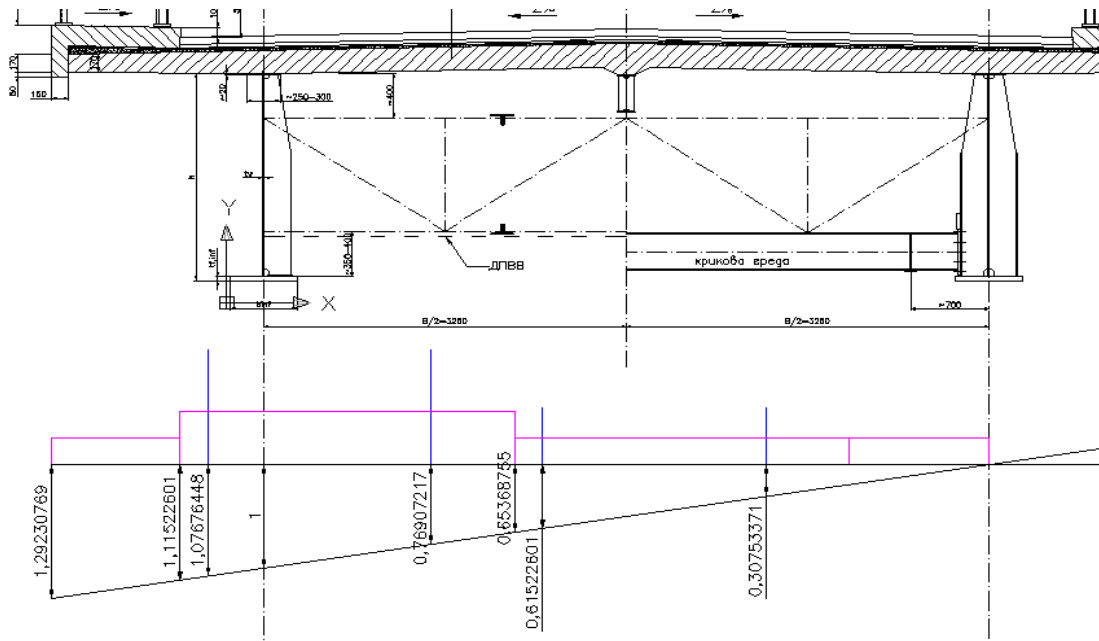


Разработил: гл. ас. д-р инж. Лазар Димитров Георгиев

**LOAD MODEL 1 - EN1991-2**



$\gamma_Q = 1.500$

$Q_{1k} = 300.00 \text{ kN}$        $Q_{2k} = 200.00 \text{ kN}$        $q_{RAk} = 2.50 \text{ kN/m}^2$

$\alpha_{1Q} = 1.00$        $\alpha_{2Q} = 1.00$        $\alpha_{RA} = 1.00$

$Q_1 = 450.00 \text{ kN}$        $Q_2 = 300.00 \text{ kN}$        $q_{RA} = 3.75 \text{ kN/m}^2$

$q_{1k} = 9.00 \text{ kN/m}^2$        $q_{2k} = 2.50 \text{ kN/m}^2$

$\alpha_{1q} = 1.00$        $\alpha_{2q} = 1.00$

$q_1 = 13.50 \text{ kN/m}^2$        $q_2 = 3.75 \text{ kN/m}^2$

Q [kN]	$\eta$	R(Q)
225.00	1.07676	242.27
225.00	0.76907	173.04
150.00	0.61523	92.28
150.00	0.30753	46.13
$R_{TL}[\text{kN}] =$		553.73
$q_{TL}[\text{kN/m}^2] =$		922.88

q [kN]	$\Omega$	R(Q)
13.50	2.65337	35.82
3.75	1.38875	5.21
3.75	1.38557	5.20
$R_{UDL}[\text{kN/m}^2] =$		46.22

**Натоварване от G2 за втори етап на работа - за една главна греда**

	b[m]	h[m]	A [m <sup>2</sup> ]	$\gamma[\text{kN/m}^3]$	$g_{2k} [\text{kN/m}]$	$g_2 [\text{kN/m}]$
Асфалтобетон + предп. Бетон	4.000	0.110	0.44000	24.000	10.560	14.256
Хидроизолация	4.000	-	-	-	1.200	1.620
Тротоарен блок	-	-	0.27563	25.000	6.891	9.302
Еластична ограда	-	-	-	-	0.700	0.945
Парапет					1.000	1.350
$g_2 [\text{kN/m}^2] =$						27.473

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 КОМБИНИРАН СТОМАНОСТОМАНОБЕТОНОВ МОСТ.

Разработил: гл. ас. д-р инж. Лазар Димитров Георгиев

**1. МАТЕРИАЛИ / MATERIALS:**

**1.1. Стомана / Steel:**

**S355J2**

$E_s = 210000 \text{ N/mm}^2$

$t_{\max} = 40 \text{ mm}$  - дебелина / thickness

$f_y = 345.00 \text{ N/mm}^2$

$f_{yd} = 328.57 \text{ N/mm}^2$

$\gamma_M = 1.050$

$f_u = 450.00 \text{ N/mm}^2$

Designation		Minimum yield strength $R_{eH}^a$ MPa <sup>b</sup>									Tensile strength $R_m^a$ MPa <sup>b</sup>				
		Nominal thickness mm									Nominal thickness mm				
According EN 10027-1 and CR 10260	According EN 10027-2	≤ 16	> 16 ≤ 40	> 40 ≤ 63	> 63 ≤ 80	> 80 ≤ 100	> 100 ≤ 150	> 150 ≤ 200	> 200 ≤ 250	> 250 ≤ 400 <sup>c</sup>	< 3	≥ 3 ≤ 100	> 100 ≤ 150	> 150 ≤ 250	> 250 ≤ 400 <sup>c</sup>
S235JR	1.0038	235	225	215	215	215	195	185	175	-	360 to 510	360 to 510	350 to 500	340 to 490	-
S235J0	1.0114	235	225	215	215	215	195	185	175	-	360 to 510	360 to 510	350 to 500	340 to 490	-
S235J2	1.0117	235	225	215	215	215	195	185	175	165	360 to 510	360 to 510	350 to 500	340 to 490	330 to 480
S275JR	1.0044	275	265	255	245	235	225	215	205	-	430 to 580	410 to 560	400 to 540	380 to 540	-
S275J0	1.0143	275	265	255	245	235	225	215	205	-	430 to 580	410 to 560	400 to 540	380 to 540	-
S275J2	1.0145	275	265	255	245	235	225	215	205	195	430 to 580	410 to 560	400 to 540	380 to 540	380 to 540
S355JR	1.0045	355	345	335	325	315	295	285	275	-	510 to 680	470 to 630	450 to 600	450 to 600	-
S355J0	1.0553	355	345	335	325	315	295	285	275	-	510 to 680	470 to 630	450 to 600	450 to 600	-
S355J2	1.0577	355	345	335	325	315	295	285	275	265	510 to 680	470 to 630	450 to 600	450 to 600	450 to 600
S355K2	1.0596	355	345	335	325	315	295	285	275	265	510 to 680	470 to 630	450 to 600	450 to 600	450 to 600
S450J0 <sup>d</sup>	1.0690	450	430	410	390	380	380	-	-	-	-	550 to 720	530 to 700	-	-

<sup>a</sup> For plate, strip and wide flats with widths ≥ 600 mm the direction transverse (t) to the rolling direction applies. For all other products the values apply for the direction parallel (l) to the rolling direction.

<sup>b</sup> 1 MPa = 1 N/mm<sup>2</sup>.

<sup>c</sup> The values apply to flat products.

**1.2. Бетон / Concrete:**

**C35/45**

$f_{ck} = 35.00 \text{ N/mm}^2$

$f_{cm} = 43.00 \text{ N/mm}^2$

$f_{ctm} = 3.21 \text{ N/mm}^2$

$f_{ctk,0.05} = 2.25 \text{ N/mm}^2$

$f_{ctk,0.95} = 2.92 \text{ N/mm}^2$

$E_{cm} = 34077 \text{ N/mm}^2$

$f_{cm} = f_{ck} + 8 \text{ (MPa)}$

$f_{ctm} = 0.30 \times f_{ck}^{(2/3)} \leq C50/60$   
 $f_{ctm} = 2.12 \cdot \ln(1 + (f_{cm}/10))$   
 $> C50/60$

$f_{ctk,0.05} = 0.7 \times f_{ctm}$   
 5% fractile

$f_{ctk,0.95} = 1.3 \times f_{ctm}$   
 95% fractile

$E_{cm} = 22[(f_{cm})/10]^{0.3}$   
 $(f_{cm} \text{ in MPa})$

**3. Геометрични характеристики на напречното сечение / geometric characteristics of cross section:**

**3.1. Стоманено сечение / Steel cross section**

$b_{fsup} = 280 \text{ mm}$

$b_{finf} = 700 \text{ mm}$

$t_{fsup} = 20 \text{ mm}$

$t_{finf} = 35 \text{ mm}$

$h_w = 2200 \text{ mm}$

$t_w = 18 \text{ mm}$

$\lambda_w = 122.22$

Разработил: гл. ас. д-р инж. Лазар Димитров Георгиев

### 3.2. Стоманобетонно сечение / Reinforced concrete cross section

$L = 33.000$  m - отвор на моста  
 $k_e = 1.000$   
 $L_e = 33.000$  m - ефективна дължина  
 $b_{os} = 0.160$  m - разстояние между крайните дюбели в напречна посока

	$b_o$ [m]	$1/8L_e$ [m]	$b_e$ [m]
Лява страна	1.670	4.125	1.670
Дясна страна	3.170	4.125	3.170

$\Sigma = 4.840$

$b_{eff} = 5000$  mm  
 $h_c = 250$  mm

### 4. Характеристики за съсъхване и пълзене / shrinkage and creep characteristics:

$A_c = 1.250$  m<sup>2</sup>  
 $u = 10.220$  m  
 $2A_c/u = 244.62$  mm

RH = 80.000 % relative humidity

TIME	$t_o$ [days]	$t$ [days]
съсъхване / shrinkage	1	36500
пълзене / creep - $g_2 + R_{op}$	90	36500

$\Psi_{AS} = 0.550$

$\Psi_{AL} = 1.100$

$(1 + \Psi_{AS} \phi_t)^{-1} = 0.383$

$(1 + \Psi_{AL} \phi_t)^{-1} = 0.419$

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### ОПРЕДЕЛЯНЕ НА ПРЕВОДНОТО ЧИСЛО ЗА СЪСЪХВАНЕ $n_{AS}$

Concrete C35/45

$f_{cm} = 43.00 \text{ N/mm}^2$        $\varphi(t, t_0) = \varphi_0 \cdot \beta_c(t, t_0)$

$f_{ck} = 35.00 \text{ N/mm}^2$       where:

$\varphi_0$  is the notional creep coefficient and may be estimated from:

$E_{cm} = 34077 \text{ N/mm}^2$        $\varphi_0 = \varphi_{RH} \cdot \beta(f_{cm}) \cdot \beta(t_0)$

Steel S235

$f_y = 345.00 \text{ N/mm}^2$

$\beta(f_{cm}) = \frac{16,8}{\sqrt{f_{cm}}}$

$\beta(t_0) = \frac{1}{(0,1 + t_0^{0,20})}$

$E_s = 210000 \text{ N/mm}^2$

$n_o = E_s / E_{cm} = 6.162$

Short-term modular ratio

$t = 36500$  days - considered time

$t_0 = 1$  days - time of load application (after concreting)

$RH = 80$  % - relative humidity

$A_c = 1.250 \text{ m}^2$  - concrete area

$u = 10.220 \text{ m}$  - concrete perimeter exposed to drying

$h_0 = 2A_c / u = 244.62 \text{ mm}$

$\alpha_1 = 0.8658$        $\beta_H = 1,5 [1 + (0,012 RH)^{18}] h_0 + 250 \leq 1500$       for  $f_{cm} \leq 35$

$\alpha_2 = 0.9597$        $\beta_H = 1,5 [1 + (0,012 RH)^{18}] h_0 + 250 \alpha_3 \leq 1500 \alpha_3$       for  $f_{cm} \geq 35$

$\alpha_3 = 0.9022$        $\alpha_{1/2/3}$  are coefficients to consider the influence of the concrete strength:

$\alpha_1 = \left[ \frac{35}{f_{cm}} \right]^{0,7}$        $\alpha_2 = \left[ \frac{35}{f_{cm}} \right]^{0,2}$        $\alpha_3 = \left[ \frac{35}{f_{cm}} \right]^{0,5}$

$\beta_H = 768.45571_0$

$\beta_c(t-t_0) = 0.9938$

$\varphi_{RH} = 1 + \frac{1 - RH/100}{0,1 \cdot \sqrt[3]{h_0}}$       for  $f_{cm} \leq 35 \text{ MPa}$

$\varphi_{RH} = 1.2657$

$\varphi_{RH} = \left[ 1 + \frac{1 - RH/100}{0,1 \cdot \sqrt[3]{h_0}} \cdot \alpha_1 \right] \cdot \alpha_2$       for  $f_{cm} > 35 \text{ MPa}$

$\beta_{f_{cm}} = 2.5620$

$\beta_{t_0} = 0.90909$

$\beta_c(t, t_0) \dots = \left[ \frac{(t - t_0)}{(\beta_H + t - t_0)} \right]^{0,3}$

$\varphi_t = 2.9296$

$\Psi_{AS} = 0.55$

Permanent loads	1.1
Shrinkage	0.55
Imposed deformations	1.5

$n_o = 6.162$

Short-term modular ratio

$1 + \Psi_L \varphi_t = 2.6113$

$n_{AS} = n_o (1 + \Psi_{AS} \varphi_t) = 16.092$

Shrinkage modular ratio

$(1 + \Psi_{AS} \varphi_t)^{-1} = 0.3830$

$E_{c,AS} = E_s / n = 13050.10 \text{ N/mm}^2 = 13050101 \text{ kN/m}^2$

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**Determining the drying shrinkage**

$f_{cm} = 43.00 \text{ N/mm}^2$

$f_{cm0} = 10.00 \text{ N/mm}^2$

$\alpha_{ds1} = 4$

$\alpha_{ds2} = 0.12$

$RH = 80.00 \%$

$RH_0 = 100 \%$

$\beta_{RH} = -0.7564$

$\epsilon_{cd,infinite} = -0.000253$

$$\epsilon_{cd,\infty} = 0,85 \left[ (220 + 110 \cdot \alpha_{ds1}) \cdot \exp\left(-\alpha_{ds2} \cdot \frac{f_{cm}}{f_{cm0}}\right) \right] \cdot 10^{-6} \cdot \beta_{RH}$$

$$\beta_{RH} = -1,55 \left[ 1 - \left( \frac{RH}{RH_0} \right)^3 \right]$$

where:

$f_{cm}$  is the mean compressive strength (MPa)

$f_{cm0} = 10 \text{ Mpa}$

$\alpha_{ds1}$  is a coefficient which depends on the type of cement  
 = 3 for slowly hardening cements (S)  
 = 4 for normal or rapid hardening cements (N)  
 = 6 for rapid hardening high-strength cements (R)

$\alpha_{ds2}$  is a coefficient which depends on the type of cement  
 = 0,13 for slowly hardening cements (S)  
 = 0,12 for normal or rapid hardening cements (N)  
 = 0,11 for rapid hardening high-strength cements (R)

$RH$  is the ambient relative humidity (%)

$RH_0 = 100\%$ .

**Autogenous shrinkage**

$\epsilon_{ca,infinite} = -0.000063$

$t = 36500 \text{ days}$

$t_s = 1 \text{ days}$

$h_0 = 244.62 \text{ mm}$

$k_h = 0.8000$

$\beta_{ds} = 0.99582462$

$h_0$	$k_h$
100	1.0
200	0.85
300	0.75
$\geq 500$	0.70

$\epsilon_{ct} = -0.000202$

$\epsilon_{sh,tot} = -0.000316 = -0.3158 \cdot 10^{-3}$  - total shrinkage

$\alpha_{tc} = 1.000E-05 \text{ K}^{-1}$  coefficient of thermal expansion for concrete

$\Delta T_{sh} = -31.5790 \text{ K}$  - equivalent temperature change for shrinkage

$E_{sh} = 13050101 \text{ kN/m}^2$  - notional modulus of elasticity for shrinkage

$\Delta T_{sh,design} = -31.5790 \text{ K}$

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### ОПРЕДЕЛЯНЕ НА ПРЕВОДНОТО ЧИСЛО ЗА ПЪЛЗЕНЕ $n_{AL}$

Concrete C35/45

$f_{cm} = 43.00 \text{ N/mm}^2$       $\varphi(t, t_0) = \varphi_0 \cdot \beta_c(t, t_0)$

$f_{ck} = 35.00 \text{ N/mm}^2$      where:

$\varphi_0$  is the notional creep coefficient and may be estimated from:

$E_{cm} = 34077 \text{ N/mm}^2$       $\varphi_0 = \varphi_{RH} \cdot \beta(f_{cm}) \cdot \beta(t_0)$

Steel S355J2

$f_y = 345.00 \text{ N/mm}^2$

$\beta(f_{cm}) = \frac{16,8}{\sqrt{f_{cm}}}$

$\beta(t_0) = \frac{1}{(0,1 + t_0^{0,20})}$

$E_s = 210000 \text{ N/mm}^2$

$n_0 = E_s/E_{cm} = 6.162$

Short-term modular ratio

$t = 36500$  days - considered time

$t_0 = 90$  days - time of load application (after concreting)

$RH = 80$  % - relative humidity

$A_c = 1.250 \text{ m}^2$  - concrete area

$u = 10.220 \text{ m}$  - concrete perimeter exposed to drying

$h_0 = 2A_c/u = 244.62 \text{ mm}$

$\alpha_1 = 0.8658$

$\beta_H = 1,5 [1 + (0,012 RH)^{18}] h_0 + 250 \leq 1500$  for  $f_{cm} \leq 35$

$\alpha_2 = 0.9597$

$\beta_H = 1,5 [1 + (0,012 RH)^{18}] h_0 + 250 \alpha_3 \leq 1500 \alpha_3$  for  $f_{cm} \geq 35$

$\alpha_3 = 0.9022$

$\alpha_{1/2/3}$  are coefficients to consider the influence of the concrete strength:

$\alpha_1 = \left[ \frac{35}{f_{cm}} \right]^{0,7}$       $\alpha_2 = \left[ \frac{35}{f_{cm}} \right]^{0,2}$       $\alpha_3 = \left[ \frac{35}{f_{cm}} \right]^{0,5}$

$\beta_H = 768.455718$

$\beta_C(t-t_0) = 0.9938$

$\varphi_{RH} = 1 + \frac{1 - RH/100}{0,1 \cdot \sqrt[3]{h_0}}$  for  $f_{cm} \leq 35 \text{ MPa}$

$\varphi_{RH} = 1.2657$

$\varphi_{RH} = \left[ 1 + \frac{1 - RH/100}{0,1 \cdot \sqrt[3]{h_0}} \cdot \alpha_1 \right] \cdot \alpha_2$  for  $f_{cm} > 35 \text{ MPa}$

$\beta_{f_{cm}} = 2.5620$

$\beta_{t_0} = 0.39070$

$\beta_c(t, t_0) \dots = \left[ \frac{(t - t_0)}{(\beta_H + t - t_0)} \right]^{0,3}$

$\varphi_t = 1.2590$

$\Psi_L = 1.10$

Permanent loads	1.1
Shrinkage	0.55
Imposed deformations	1.5

$n_0 = 6.162$

Short-term modular ratio

$1 + \Psi_L \varphi_t = 2.3849$

$n_{AL} = n_0(1 + \Psi_L \varphi_t) = 14.697$

Creep modular ratio

$(1 + \Psi_{AL} \varphi_t)^{-1} = 0.4193$

$E_{c,AS} = E_s/n = 14288.61 \text{ N/mm}^2 = 14288609 \text{ kN/m}^2$

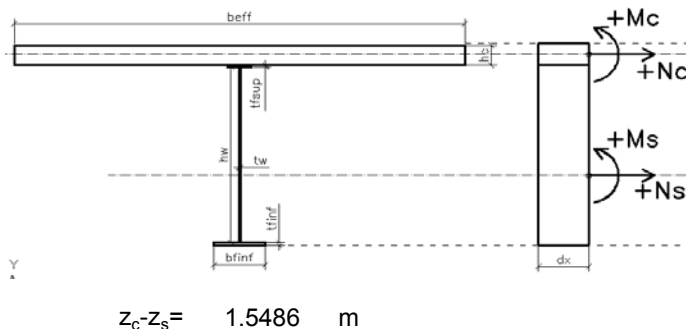
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**SECTION x= 16.500 m**

**ИЗЧИСЛЕНИЕ ЗА СЪСЪХВАНЕ / SHRINKAGE CALCULATIONS**

$\epsilon_{sh}$ =	-0.00031579	shrinkage deformation	
$E_s$ =	210000000 kN/m <sup>2</sup>	=	21000.00 kN/cm <sup>2</sup>
$E_c$ =	13050101 kN/m <sup>2</sup>	=	1305.01 kN/cm <sup>2</sup>
$n_{AS}$ =	16.09183		
$b_{eff}$ =	500.0 cm		
$h_c$ =	25.0 cm		
$b_{fsup}$ =	28.0 cm	$b_{finf}$ =	70.0 cm
$t_{fsup}$ =	2.0 cm	$t_{finf}$ =	3.5 cm
$h_w$ =	220.0 cm	$h_{out}$ =	2.255 m
$t_w$ =	1.8 cm		

$A_s$ =	697.0 cm <sup>2</sup>
$J_s$ =	4704463.4 cm <sup>4</sup>
$z_s$ =	83.1 cm
$A_c$ =	12500.0 cm <sup>2</sup>
$J_c$ =	651041.7 cm <sup>4</sup>
$z_c$ =	238.0 cm
$z_i$ =	164.7609 cm
$A_i$ =	1473.7917 cm <sup>2</sup>
$J_i$ =	13555298.39 cm <sup>4</sup>



$N_{s,sh}$ =	-852.78 kN
$M_{s,sh}$ =	1309.38 kNm

**Partial internal forces for steel section /**  
**Частни разрезни усилия за стоманеното сечение**

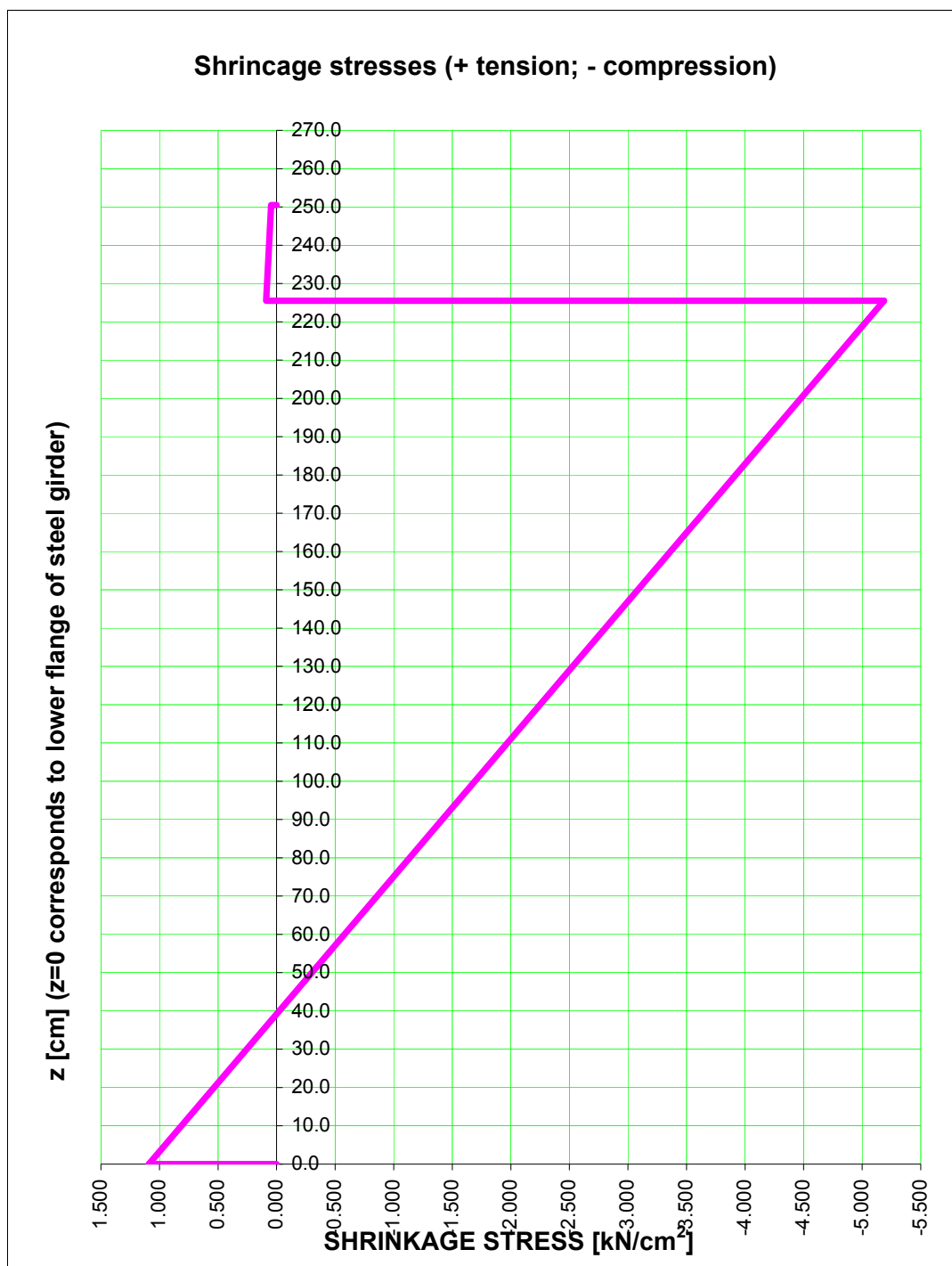
$N_{c,sh}$ =	852.78 kN
$M_{c,sh}$ =	11.26 kNm

**Partial internal forces for RC section /**  
**Частни разрезни усилия за ст.б. сечение**

F1=	0.00000000E+00 =0;	$N_c + N_s = 0$
F2=	0.00000000E+00 =0;	$M_s + M_c + N_s(z_i - z_s) - N_c(z_c - z_i) = 0$
F3=	1.00000000E-10 =0;	$[\epsilon_{sh} + N_c / (E_c A_c) + M_c z_c / (E_c J_c)] - [N_s / (E_s A_s) - M_s z_s / (E_s J_s)] = 0$
F4=	-2.36963366E-11 =0;	$(M_c / M_s) - (J_c / n_{sh}) / J_s = 0$

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z [cm]	$\sigma_{sh}$ [kN/cm <sup>2</sup> ]	$z_s$ [cm]	$\sigma_{sh}(N)$	$\sigma_{sh}(M)$
0.00	1.09044	83.137	-1.224	2.314
225.50	-5.18586	-142.363	-1.224	-3.962
225.50	0.08984	12.500	0.068	0.022
250.50	0.04660	-12.500	0.068	-0.022





Разработил: гл. ас. д-р инж. Лазар Димитров Георгиев

**SECTION x= 16.500 m**

**CREEP CALCULATIONS**

$g_2 = 27.473$  kN/m                       $R = 637.77$  kN  
 $L = 33.000$  m                               $L_1 = 11.000$  m  
 $M_m = 10755.29$  kNm  
 $E_s = 210000000$  kN/m<sup>2</sup>                      =                       $21000.00$  kN/cm<sup>2</sup>  
 $E_c = 14288609$  kN/m<sup>2</sup>                      =                       $1428.86$  kN/cm<sup>2</sup>  
 $n_{AL} = 14.69702$

$b_{eff} = 500.0$  cm

$h_c = 25.0$  cm

$b_{fsup} = 28.0$  cm

$b_{finf} = 70.0$  cm

$t_{fsup} = 2.0$  cm

$t_{finf} = 3.5$  cm

$h_w = 220.0$  cm

$t_w = 1.8$  cm

$A_s = 697.0$  cm<sup>2</sup>

$J_s = 4704463.4$  cm<sup>4</sup>

$z_s = 83.1$  cm

$A_c = 12500.0$  cm<sup>2</sup>

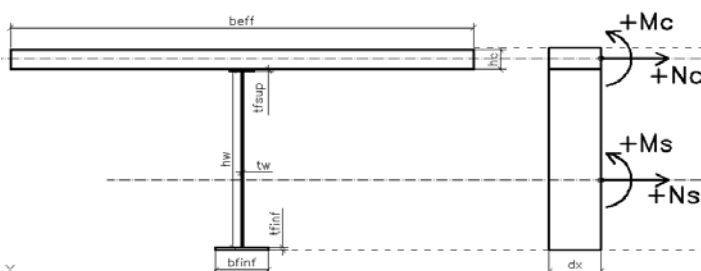
$J_c = 651041.7$  cm<sup>4</sup>

$z_c = 238.0$  cm

$z_i = 168.2498$  cm

$A_i = 1547.5124$  cm<sup>2</sup>

$J_i = 13935736.02$  cm<sup>4</sup>



$N_s = 4578.45$  kN

$M_s = 3630.80$  kNm

Partial internal forces for steel section /

Частни разрезни усилия за стоманеното сечение

$N_c = -4578.45$  kN

$M_c = 34.19$  kNm

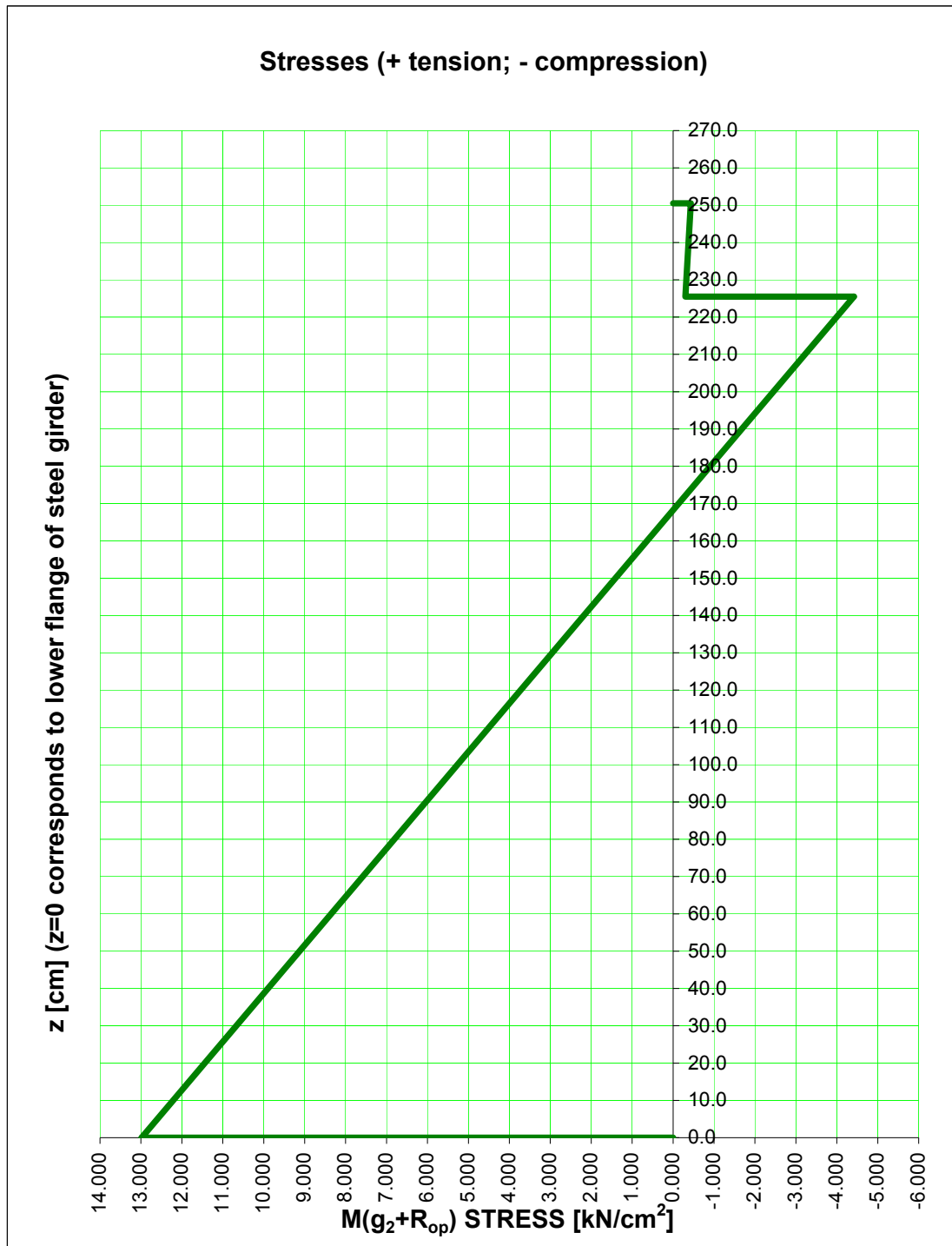
Partial internal forces for RC section /

Частни разрезни усилия за ст.б. сечение

Катедра Транспортни съоръжения, ФТС на УАСГ  
 ЧИСЛЕН ПРИМЕР ЗА ПРОВЕРКИ НА НАПРЕЖЕНИЯТА В СРЕДНОТО СЕЧЕНИЕ НА ЕДНООТВОРЕН  
 КОМБИНИРАН СТОМАНОСТОМАНОБЕТОНОВ МОСТ.

Разработил: гл. ас. д-р инж. Лазар Димитров Георгиев

z [cm]	$\sigma_{sh}$ [kN/cm <sup>2</sup> ]	$z_s$ [cm]	$\sigma_{sh}(N)$	$\sigma_{sh}(M)$
0.00	12.985	83.137	6.569	6.416
225.50	-4.418	-142.363	6.569	-10.987
225.50	-0.301	12.500	-0.366	0.066
250.50	-0.432	-12.500	-0.366	-0.066



Разработил: гл. ас. д-р инж. Лазар Димитров Георгиев

**SECTION x= 16.500 m**

CALCULATIONS - no

$g_2=$	27.473	kN/m	$R=$	637.77	kN
$L=$	33.000	m	$L_1=$	11.00	m
$M_m=$	10755.29	kNm			
$E_s=$	210000000	kN/m <sup>2</sup>	$=$	21000.00	kN/cm <sup>2</sup>
$E_c=$	34077146	kN/m <sup>2</sup>	$=$	3407.71	kN/cm <sup>2</sup>
$n_o=$	6.16249				

$b_{eff}= 500.0$  cm

$h_c= 25.0$  cm

$b_{fsup}= 28.0$  cm

$b_{finf}= 70.0$  cm

$t_{fsup}= 2.0$  cm

$t_{finf}= 3.5$  cm

$h_w= 220.0$  cm

$t_w= 1.8$  cm

$A_s= 697.0$  cm<sup>2</sup>

$J_s= 4704463.4$  cm<sup>4</sup>

$z_s= 83.1$  cm

$A_c= 12500.0$  cm<sup>2</sup>

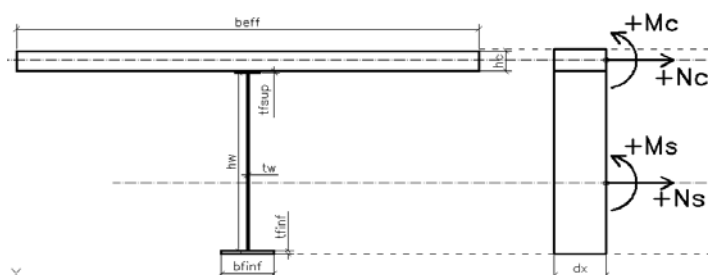
$J_c= 651041.7$  cm<sup>4</sup>

$z_c= 238.0$  cm

$z_i= 198.3951$  cm

$A_i= 2725.4016$  cm<sup>2</sup>

$J_i= 17250942.04$  cm<sup>4</sup>



$N_s= 5008.55$  kN

Partial internal forces for steel section /

$M_s= 2933.05$  kNm

Частни разрезни усилия за стоманеното сечение

$N_c= -5008.55$  kN

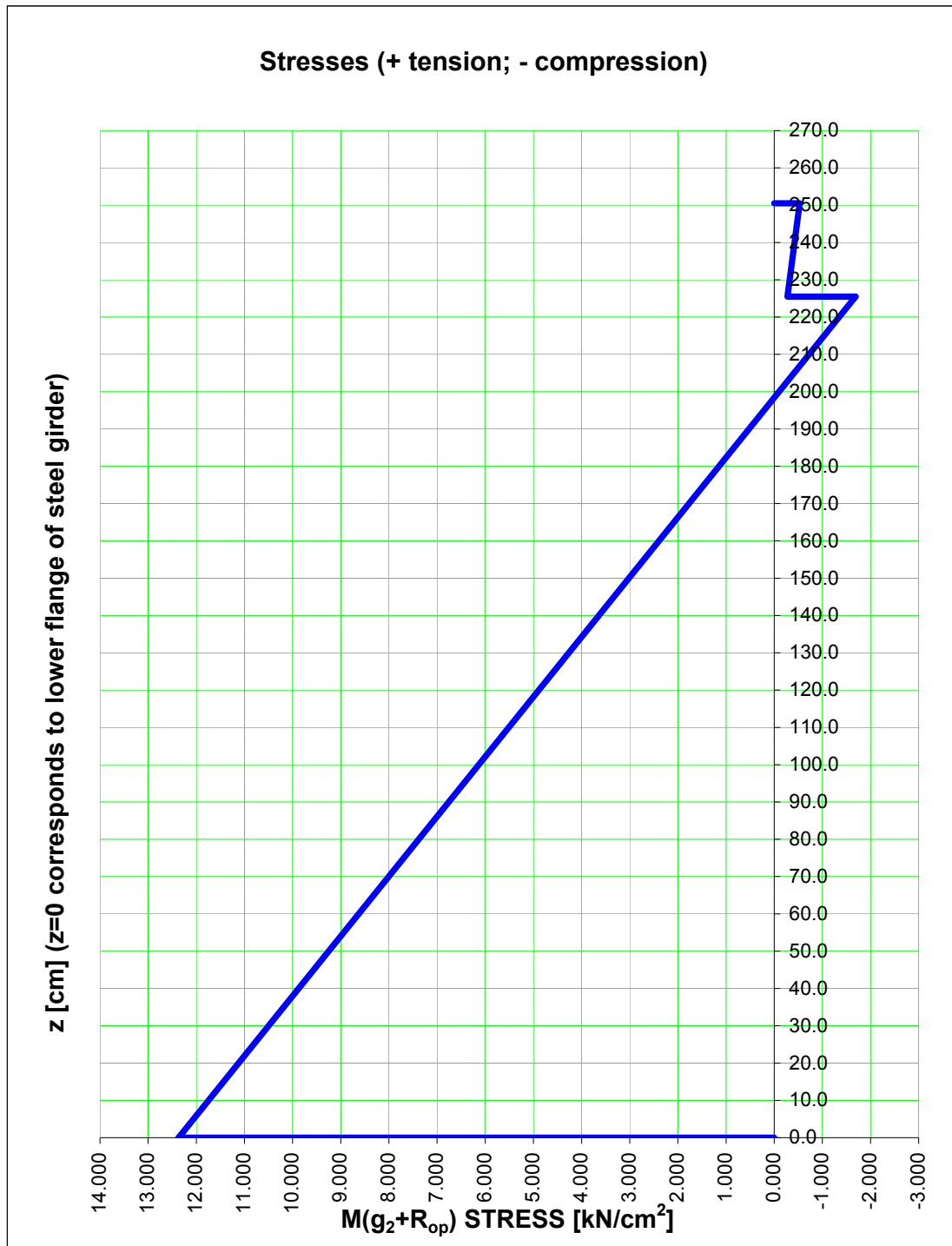
Partial internal forces for RC section /

$M_c= 65.87$  kNm

Частни разрезни усилия за ст.б. сечение

Разработил: гл. ас. д-р инж. Лазар Димитров Георгиев

z [cm]	$\sigma_{sh}$ [kN/cm <sup>2</sup> ]	$z_s$ [cm]	$\sigma_{sh}(N)$	$\sigma_{sh}(M)$
0.00	12.369	83.137	7.186	5.183
225.50	-1.690	-142.363	7.186	-8.876
225.50	-0.274	12.500	-0.401	0.126
250.50	-0.527	-12.500	-0.401	-0.126



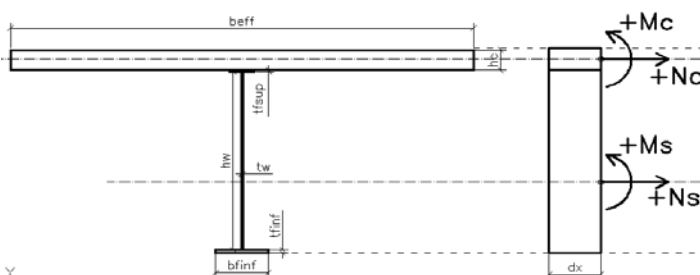
Разработил: гл. ас. д-р инж. Лазар Димитров Георгиев

**SECTION x= 16.500 m**

Напрежения от товарен модел 1 LM1 - CALCULATIONS - no

$q_{LM1\_UDL} =$	46.224	kN/m	$F_{LM1\_TL} =$	553.73	kN	$x =$	16.5
$L =$	33.000	m	$\eta_1 + \eta_2 =$	15.9			
$M_m =$	15096.53	kNm					
$E_s =$	210000000	kN/m <sup>2</sup>	$=$	21000.00	kN/cm <sup>2</sup>		
$E_c =$	34077146	kN/m <sup>2</sup>	$=$	3407.71	kN/cm <sup>2</sup>		
$n_o =$	6.16249						
$b_{eff} =$	525.0	cm					
$h_c =$	25.0	cm					
$b_{fsup} =$	28.0	cm	$b_{finf} =$	70.0	cm		
$t_{fsup} =$	2.0	cm	$t_{finf} =$	3.5	cm		
$h_w =$	220.0	cm					
$t_w =$	1.8	cm					

$A_s =$	697.0	cm <sup>2</sup>
$J_s =$	4704463.4	cm <sup>4</sup>
$z_s =$	83.1	cm
$A_c =$	13125.0	cm <sup>2</sup>
$J_c =$	683593.8	cm <sup>4</sup>
$z_c =$	238.0	cm
$z_i =$	199.8160	cm
$A_i =$	2826.8216	cm <sup>2</sup>
$J_i =$	17409599.07	cm <sup>4</sup>



$N_s =$	7052.01	kN
$M_s =$	4079.42	kNm

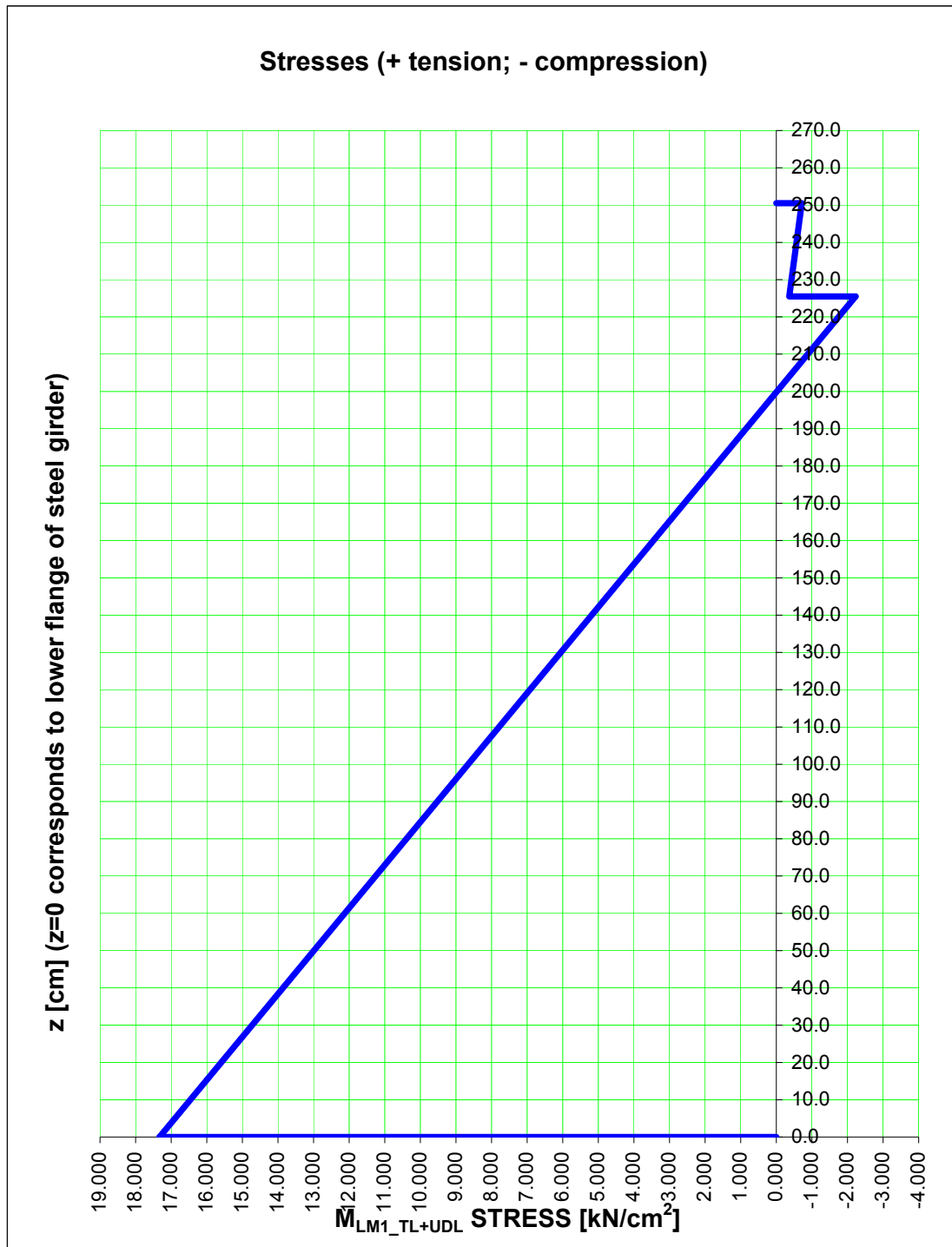
Partial internal forces for steel section /  
 Частни разрезни усилия за стоманеното сечение

$N_c =$	-7052.01	kN
$M_c =$	96.19	kNm

Partial internal forces for RC section /  
 Частни разрезни усилия за ст.б. сечение

Разработил: гл. ас. д-р инж. Лазар Димитров Георгиев

z [cm]	$\sigma_{sh}$ [kN/cm <sup>2</sup> ]	$z_s$ [cm]	$\sigma_{sh}(N)$	$\sigma_{sh}(M)$
0.00	17.327	83.137	10.118	7.209
225.50	-2.227	-142.363	10.118	-12.345
225.50	-0.361	12.500	-0.537	0.176
250.50	-0.713	-12.500	-0.537	-0.176



Разработил: гл. ас. д-р инж. Лазар Димитров Георгиев

**SECTION x= 16.500 m**

**TEMPERATURE CHANGE +15°C**

T= 15.000 °C

$\alpha_{tc}$ = 0.00001

$\varepsilon_t$ = 0.00015000

Es= 210000000 kN/m<sup>2</sup> = 21000.00 kN/cm<sup>2</sup>

E<sub>c</sub>= 34077146 kN/m<sup>2</sup> = 3407.71 kN/cm<sup>2</sup>

n<sub>sh</sub>= 6.16249

b<sub>eff</sub>= 500.0 cm

h<sub>c</sub>= 25.0 cm

b<sub>fsup</sub>= 28.0 cm      b<sub>finf</sub>= 70.0 cm

t<sub>fsup</sub>= 2.0 cm      t<sub>finf</sub>= 3.5 cm

h<sub>w</sub>= 220.0 cm

t<sub>w</sub>= 1.8 cm

As= 697.0 cm<sup>2</sup>

Js= 4704463.4 cm<sup>4</sup>

z<sub>s</sub>= 83.1 cm

A<sub>c</sub>= 12500.0 cm<sup>2</sup>

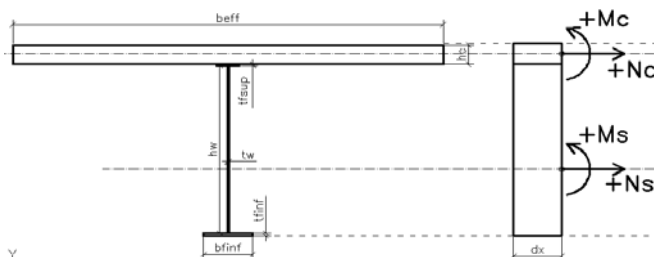
J<sub>c</sub>= 651041.7 cm<sup>4</sup>

z<sub>c</sub>= 238.0 cm

z<sub>i</sub>= 198.3951 cm

A<sub>i</sub>= 2725.4016 cm<sup>2</sup>

J<sub>i</sub>= 17250942.04 cm<sup>4</sup>



N<sub>s</sub>= 455.63 kN

M<sub>s</sub>= -690.10 kNm

Partial internal forces for steel section /

Частни разрезни усилия за стоманеното сечение

N<sub>c</sub>= -455.63 kN

M<sub>c</sub>= -15.50 kNm

Partial internal forces for RC section /

Частни разрезни усилия за ст.б. сечение

F1= 0.00000000E+00 =0;

N<sub>c</sub>+N<sub>s</sub>=0

F2= 0.00000000E+00 =0;

M<sub>s</sub>+M<sub>c</sub>+N<sub>s</sub>(z<sub>i</sub>-z<sub>s</sub>)-N<sub>c</sub>(z<sub>c</sub>-z<sub>i</sub>)=0

F3= 0.00000000E+00 =0;

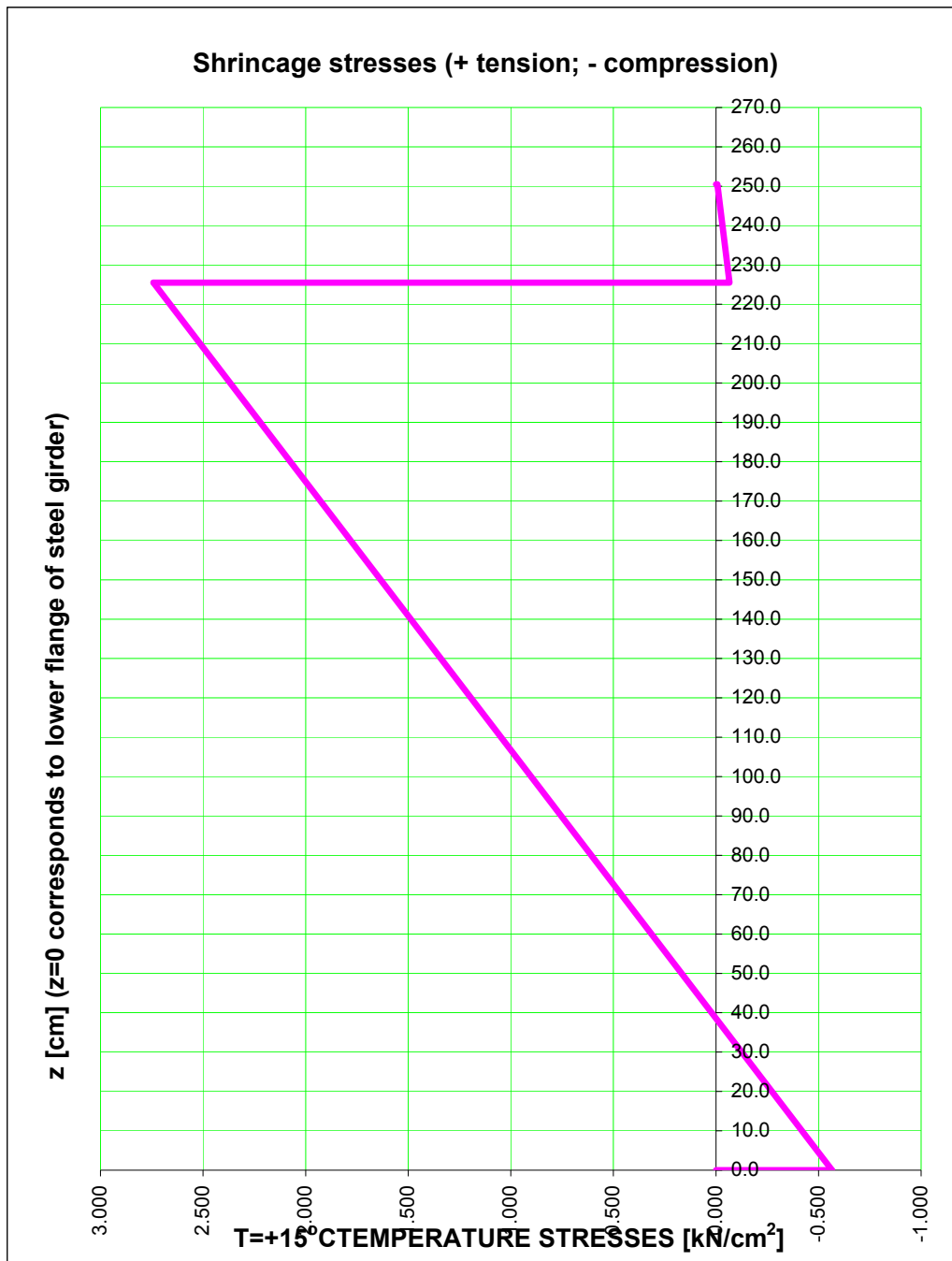
[ $\varepsilon_{sh}$ +N<sub>c</sub>/(E<sub>c</sub>A<sub>c</sub>)+M<sub>c</sub>z<sub>c</sub>/(E<sub>c</sub>J<sub>c</sub>)]-[N<sub>s</sub>/(E<sub>s</sub>A<sub>s</sub>)-M<sub>s</sub>z<sub>s</sub>/(E<sub>s</sub>J<sub>s</sub>)]=0

F4= 2.49800181E-16 =0;

(M<sub>c</sub>/M<sub>s</sub>)-((J<sub>c</sub>/n<sub>sh</sub>)/J<sub>s</sub>)=0

Разработил: гл. ас. д-р инж. Лазар Димитров Георгиев

z [cm]	$\sigma_t$ [kN/cm <sup>2</sup> ]	$z_s$ [cm]	$\sigma_{sh}(N)$	$\sigma_{sh}(M)$
0.00	-0.56585	83.137	0.654	-1.220
225.50	2.74201	-142.363	0.654	2.088
225.50	-0.06620	12.500	-0.036	-0.030
250.50	-0.00670	-12.500	-0.036	0.030





Разработил: гл. ас. д-р инж. Лазар Димитров Георгиев

**SECTION x= 16.500 m**

**TEMPERATURE CHANGE -15°C**

$T_{Ed} = -15.000$  °C

$\alpha_{tc} = 0.00001$

$\varepsilon_t = -0.00015000$

$E_s = 210000000$  kN/m<sup>2</sup> = 21000.00 kN/cm<sup>2</sup>

$E_c = 34077146$  kN/m<sup>2</sup> = 3407.71 kN/cm<sup>2</sup>

$n_{sh} = 6.16249$

$b_{eff} = 500.0$  cm

$h_c = 25.0$  cm

$b_{fsup} = 28.0$  cm  $b_{finf} = 70.0$  cm

$t_{fsup} = 2.0$  cm  $t_{finf} = 3.5$  cm

$h_w = 220.0$  cm

$t_w = 1.8$  cm

$A_s = 697.0$  cm<sup>2</sup>

$J_s = 4704463.4$  cm<sup>4</sup>

$z_s = 83.1$  cm

$A_c = 12500.0$  cm<sup>2</sup>

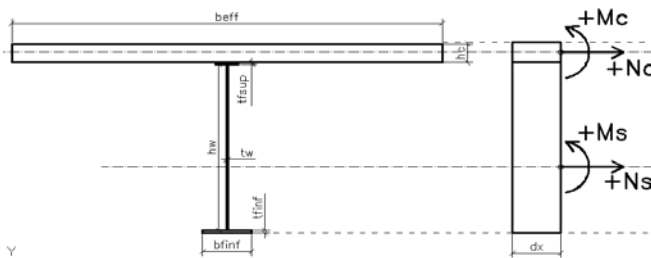
$J_c = 651041.7$  cm<sup>4</sup>

$z_c = 238.0$  cm

$z_i = 198.3951$  cm

$A_i = 2725.4016$  cm<sup>2</sup>

$J_i = 17250942.04$  cm<sup>4</sup>



$N_s = -455.63$  kN

$M_s = 690.10$  kNm

Partial internal forces for steel section /

Частни разрезни усилия за стоманеното сечение

$N_c = 455.63$  kN

$M_c = 15.50$  kNm

Partial internal forces for RC section /

Частни разрезни усилия за ст.б. сечение

$F_1 = 0.00000000E+00 = 0;$

$N_c + N_s = 0$

$F_2 = 0.00000000E+00 = 0;$

$M_s + M_c + N_s(z_i - z_s) - N_c(z_c - z_i) = 0$

$F_3 = 0.00000000E+00 = 0;$

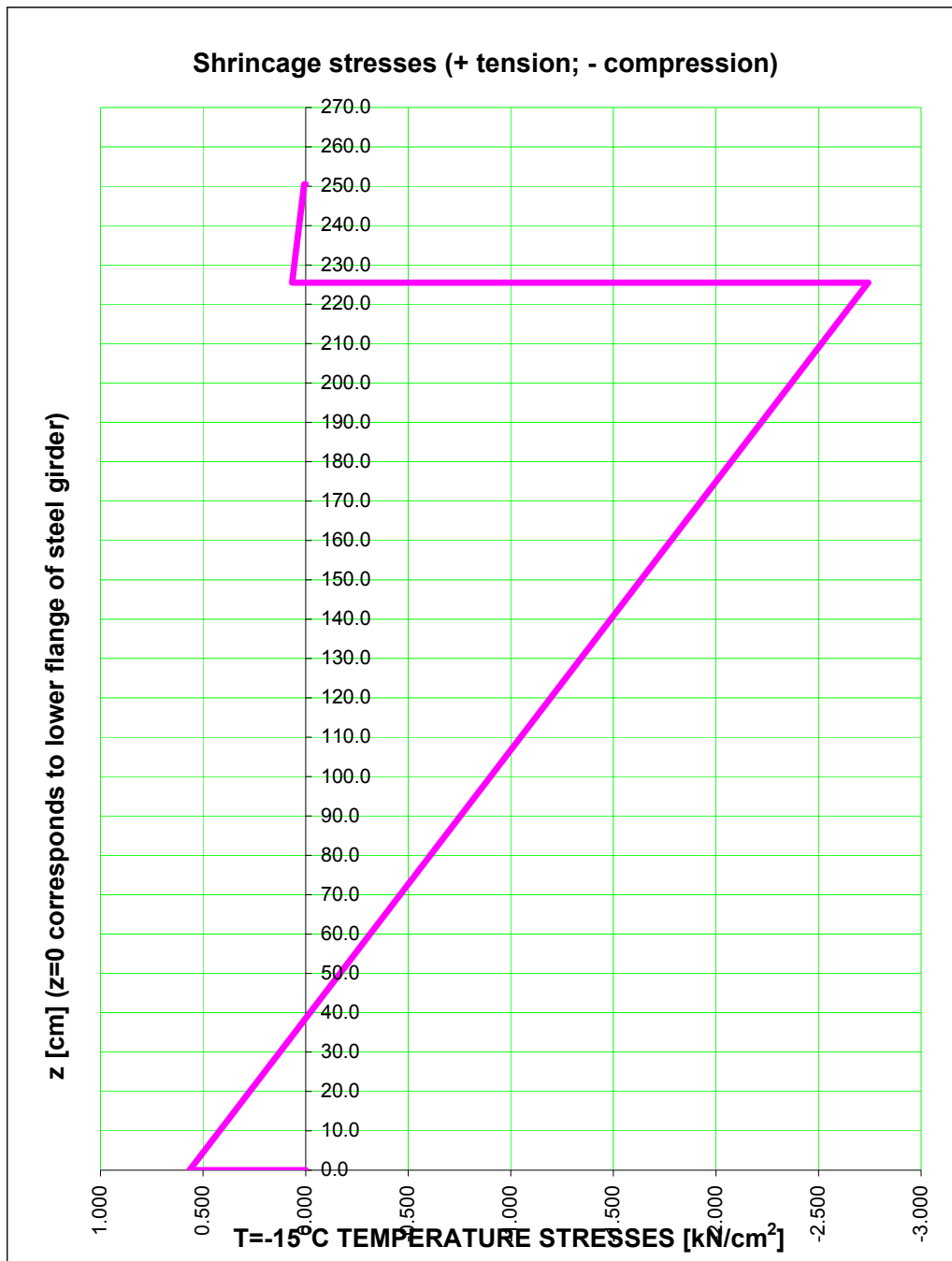
$[\varepsilon_{sh} + N_c / (E_c A_c) + M_c z_c / (E_c J_c)] - [N_s / (E_s A_s) - M_s z_s / (E_s J_s)] = 0$

$F_4 = 2.15105711E-16 = 0;$

$(M_c / M_s) - ((J_c / n_{sh}) / J_s) = 0$

Разработил: гл. ас. д-р инж. Лазар Димитров Георгиев

z [cm]	$\sigma_t$ [kN/cm <sup>2</sup> ]	$z_s$ [cm]	$\sigma_{sh}(N)$	$\sigma_{sh}(M)$
0.00	0.56585	83.137	-0.654	1.220
225.50	-2.74201	-142.363	-0.654	-2.088
225.50	0.06620	12.500	0.036	0.030
250.50	0.00670	-12.500	0.036	-0.030



**SECTION x= 16.500 m**

		НАПРЕЖЕНИЯ - ВТОРИ ЕТАП/STRESSES - STAGE 2 [kN/cm <sup>2</sup> ]						STAGE1
LOAD		LM1	G2no	G2nal	SH	TP15	TM15	[kN/cm <sup>2</sup> ]
ratio n		6.162	6.162	14.697	16.092	6.162	6.162	-
0	1	2	3	4	5	6	7	8
z [cm]	0.00	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	0.00	17.327	12.369	12.985	1.090	-0.566	0.566	0.283
	225.50	-2.227	-1.690	-4.418	-5.186	2.742	-2.742	-0.485
	225.50	-0.361	-0.274	-0.301	0.090	-0.066	0.066	0.000
	250.50	-0.713	-0.527	-0.432	0.047	-0.007	0.007	0.000
	250.50	0.000	0.000	0.000	0.000	0.000	0.000	0.000

**STRESSES - STAGE 1 + STAGE 2**

		COMB	1	2	3	4	5	6	7	8
Description			"LM1"+"G2no"+"SH"	"LM1"+"G2nal"+"SH"	"LM1"+"G2nal"+"SH" +"TM15"	"LM1"+"G2nal"+"SH" +"TP15"	"LM1"+"G2no"+"SH" +"TM15"	"LM1"+"G2no"+"SH" +"TP15"	"LM1"+"G2no"	"LM1"+"G2nal"
z [cm]	0.00	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	0.00	31.069	31.685	32.251	31.120	31.635	30.504	29.696	30.595	
	225.50	-9.588	-12.316	-15.058	-9.574	-12.330	-6.846	-3.917	-7.130	
	225.50	-0.546	-0.572	-0.506	-0.638	-0.480	-0.612	-0.636	-0.662	
	250.50	-1.194	-1.099	-1.092	-1.105	-1.187	-1.200	-1.240	-1.145	
	250.50	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	

Stage 1: Section x=L/2 "m"

M<sub>1</sub>= 160.15 kNm - with relevant sign + or -

W<sub>s,inf</sub>= 56586.6 cm<sup>3</sup>      σ<sub>1,inf</sub>= 0.283 kN/cm<sup>2</sup>

W<sub>s,sup</sub>= -33045.6 cm<sup>3</sup>      σ<sub>1,sup</sub>= -0.485 kN/cm<sup>2</sup>

f<sub>y</sub>= 35.500 kN/cm<sup>2</sup> - for t<=16mm

f<sub>y</sub>= 34.500 kN/cm<sup>2</sup> - for 16< t<=40mm      γ<sub>M0</sub>= 1.05      f<sub>yd</sub>= 32.857 kN/cm<sup>2</sup>

σ<sub>1,inf</sub>= 0.283 kN/cm<sup>2</sup>      σ<sub>sh,inf</sub>= 1.090 kN/cm<sup>2</sup>

σ<sub>2,inf</sub>= 31.484 kN/cm<sup>2</sup>      (σ<sub>2inf</sub>=f<sub>yd</sub>-σ<sub>1,inf</sub>-σ<sub>sh,inf</sub>)

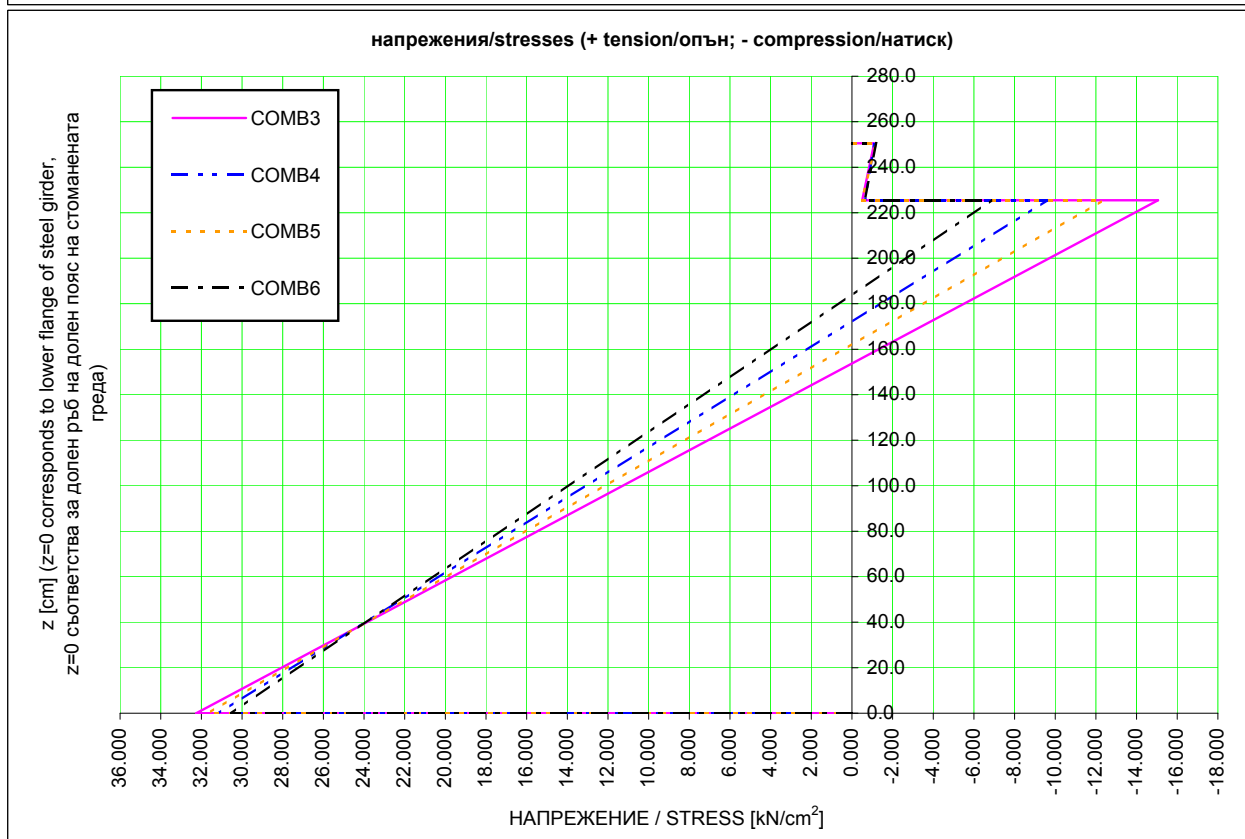
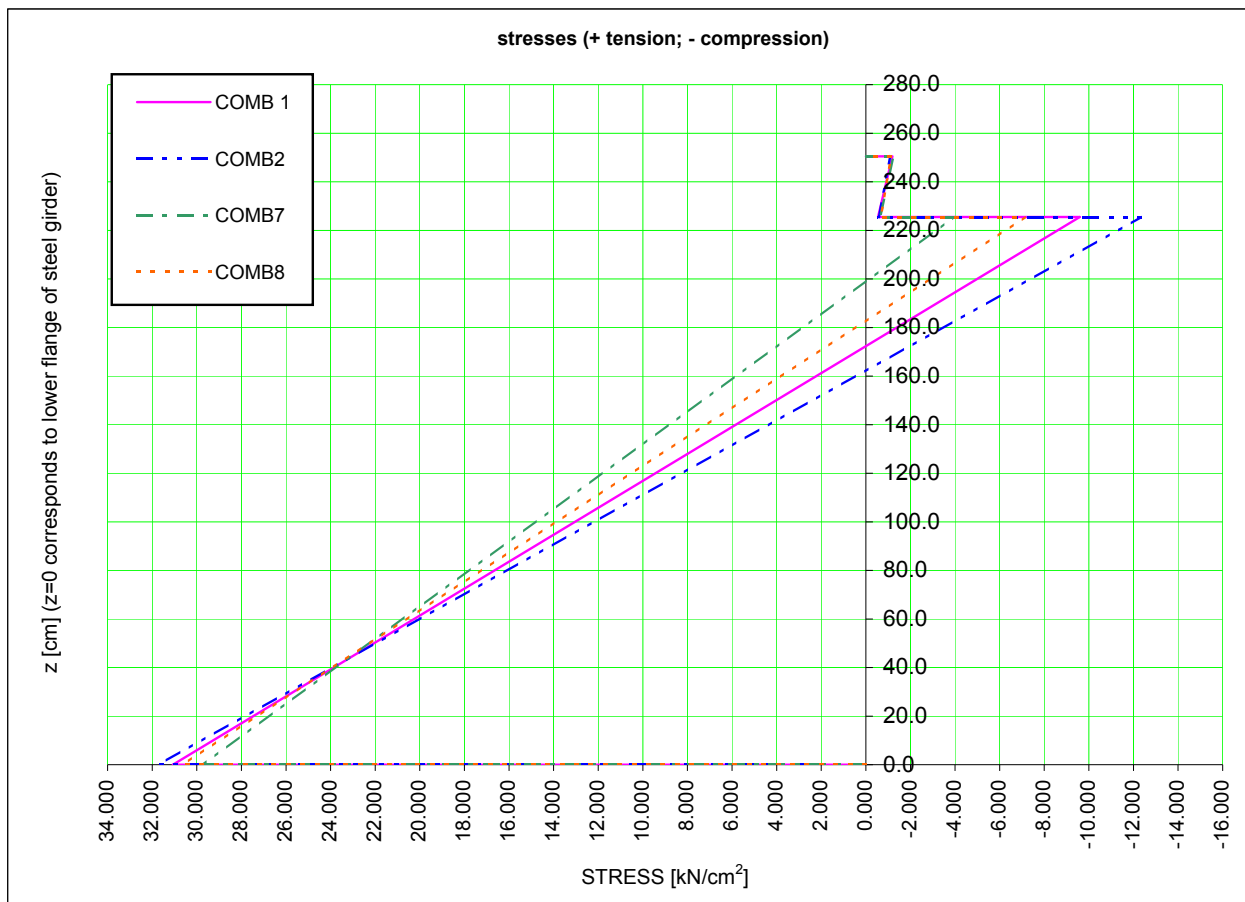
M<sub>u</sub>= 27375.84 kNm

M<sub>Ed,2,no</sub>= 25851.83 kNm

x= 16.500 m

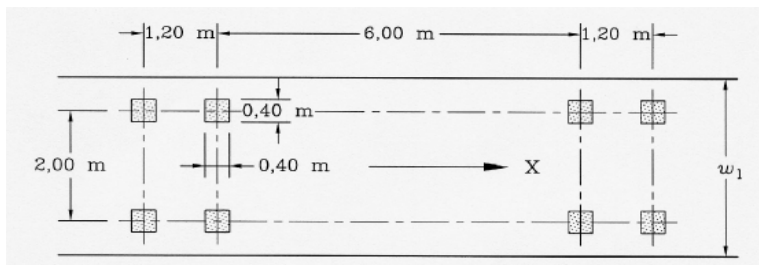
M<sub>u</sub>/M<sub>Ed</sub>= 1.0590

Разработил: гл. ас. д-р инж. Лазар Димитров Георгиев



**В: Проверки на умора за дюбелната връзка между стоманобетонна плоча и стоманена греда за средата на отвора: разработил: гл. ас. д-р инж. Лазар Димитров Георгиев**

1. EN1991-2: FLM3 и честота  $0,5 \cdot 10^6$  возила/година



$Q_{FLM3,k} = 120.00 \text{ kN/oc}$

Параметри на мостовата конструкция

- $B = 6.500 \text{ m}$  - разстояние между осите на гл.н.
- $l_k = 1.750 \text{ m}$  - конзолно издаване
- $G = 10.000 \text{ m}$  - габарит на пътната конструкция
- $L = 33.000 \text{ m}$  - отвор на мостовата конструкция

**2. Статическо решение**

2.1. Решение в напречна посока

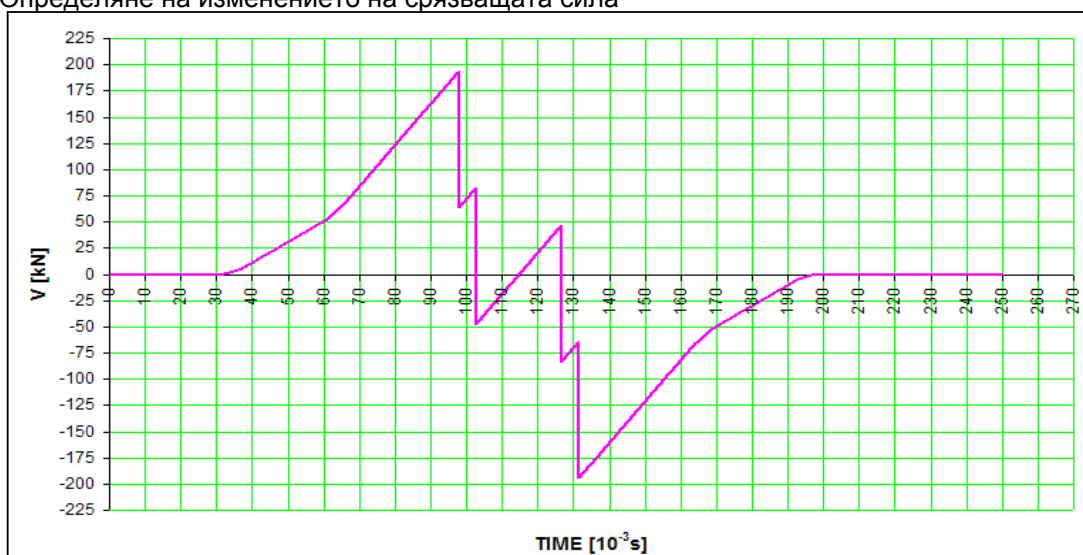
$\eta_1 = 1.23846$

$\eta_2 = 0.93077$

$\Sigma \eta_i = 2.16923$

$P_{FLM3} = 130.15 \text{ kN}$  за едната главна греда

2.2. Определяне на изменението на срязващата сила



Разработил: гл. ас. д-р инж. Лазар Димитров Георгиев



УАСГ – София  
 Факултет по ТРАНСПОРТНО СТРОИТЕЛСТВО  
 Катедра “ТРАНСПОРТНИ СЪОРЪЖЕНИЯ”  
 Специалност СТС4

**ЧИСЛЕН ПРИМЕР: Проверки на умора за дюбелната връзка между стоманобетонна плоча и стоманена греда за средата на отвора: разработил: гл. ас. д-р инж. Лазар Димитров Георгиев**

$$E_s = 210000000 \text{ kN/m}^2 = 21000.00 \text{ kN/cm}^2$$

$$E_c = 34077146 \text{ kN/m}^2 = 3407.71 \text{ kN/cm}^2$$

$$n = 6.16249 = n_0$$

$$b_{\text{eff}} = 500.0 \text{ cm} \quad b_{\text{cred}} = 81.1 \text{ cm}$$

$$h_c = 25.0 \text{ cm}$$

$$b_{\text{fsup}} = 40.0 \text{ cm} \quad b_{\text{finf}} = 85.0 \text{ cm}$$

$$t_{\text{fsup}} = 2.0 \text{ cm} \quad t_{\text{finf}} = 4.0 \text{ cm}$$

$$h_w = 300.0 \text{ cm}$$

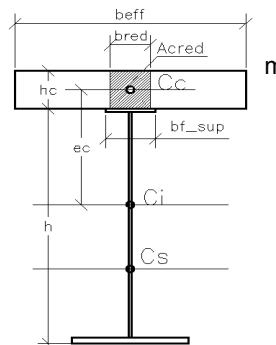
$$t_w = 2.0 \text{ cm}$$

$$A_s = 1020.0 \text{ cm}^2$$

$$J_s = 12642508.2 \text{ cm}^4$$

$$z_s = 115.2 \text{ cm}$$

$$S_{si} = 137997.0 \text{ cm}^3$$



$$A_c = 12500.0 \text{ cm}^2 \quad A_{\text{cred}} = 2028.4 \text{ cm}^2$$

$$J_c = 651041.7 \text{ cm}^4 \quad J_{\text{cred}} = 105645.9 \text{ cm}^4$$

$$z_c = 318.5 \text{ cm} \quad z_c - z_s = 2.0332 \text{ m}$$

$$S_{s,ci} = -137997.0 \text{ cm}^3$$

$$z_i = 250.5 \text{ cm}$$

$$A_i = 3048.4016 \text{ cm}^2$$

$$J_i = 40806186.5 \text{ cm}^4$$

$$S_{\text{cred},ci} = 137997.0 \text{ cm}^3$$

$$S_{\text{cred},ci} / J_i = 0.0033818 \text{ cm}^{-1}$$

$$d = 19 \text{ mm} \text{ - диаметър на дюбелите} \quad 5d = 95 \text{ mm}$$

$$n_p = 2 \text{ брой дюбели в напречен ред}$$

$$l_s = 180 \text{ mm} \text{ - надлъжно разстояние между дюбелите}$$

$$n_1 = 11.111 \text{ броя / m'}$$

**ЧИСЛЕН ПРИМЕР: Проверки на умора за дюбелната връзка между стоманобетонна плоча и стоманена греда за средата на отвора:**

$$A_d = 2.8353 \text{ cm}^2$$

$$\Delta\tau = K_v \cdot \Delta V$$

$$K_v = 107.34677 \text{ m}^{-2}$$

$$K_v = \frac{S_{c,red,Ci}}{I_i \cdot n_1 \cdot A_d} \gamma_{F,f} = \frac{4 \cdot S_{c,red,Ci}}{I_i \cdot n_1 \cdot \pi \cdot d^2} \gamma_{F,f}$$

$$\Delta\tau_c = 90.000 \text{ N/mm}^2 = 90000 \text{ kN/m}^2$$

$$m = 8.00$$

$$\Delta\tau_{c,FL} = 55.191 \text{ N/mm}^2$$

$$\gamma_{Ff} = 1.150$$

$$\gamma_{Mf} = 1.350$$

DAMAGE TOLERANT	SAFE LIFE	-
1.000	1.150	$\gamma_{Ff}$
1.150	1.350	$\gamma_{Mf}$

$\Delta V$ [kN]	387.70	94.26	18.54	18.54
$\Delta\tau$ [kN/cm <sup>2</sup> ]	4.162	1.012	0.199	0.199
$\Delta\tau_c$ [kN/cm <sup>2</sup> ]	6.667	6.667	6.667	6.667
$\Delta\tau_{c,FL}$ [kN/cm <sup>2</sup> ]	4.088	4.088	4.088	4.088
$n_{i,1}$ [цикли/год]	5.000E+05	5.000E+05	5.000E+05	5.000E+05
$N_i$ [цикли]	8.670E+07	1.000E+40	1.000E+40	1.000E+40
$D_{i1}$	0.005767	0.000000	0.000000	0.000000
	$D_1 =$			0.005767
Експлоатационен срок T [год] =				173.40

